Tutorial 7

December 14, 2015

In this week's tutorial we will study the invariance of the Standard Model Lagrangian under the C, P and T symmetries. The Higgs, gluon and electromagnetic interactions are independently invariant under C, P and CP (which is equivalent to T, given that CPT is always a symmetry). The neutral-current couplings to the Z boson break C and P but are symmetric under CP.

Here, we will study the charged-current couplings to the W boson, focusing on the Lagrangian term describing the quark interactions,

$$\mathcal{L}_{q}^{W} = \frac{ig_{2}}{2\sqrt{2}} \left[V_{mn} W_{\mu}^{\dagger} \bar{u}_{m} \gamma^{\mu} (1+\gamma_{5}) d_{n} + (V^{\dagger})_{mn} W_{\mu}^{-} \bar{d}_{m} \gamma^{\mu} (1+\gamma_{5}) u_{n} \right].$$
(1)

Using

$$\mathcal{C}W^{\pm}_{\mu}\mathcal{C}^* = -W^{\mp}_{\mu} \qquad \mathcal{P}W^{\pm}_{\mu}\mathcal{P}^* = P^{\nu}_{\ \mu}W^{\pm}_{\nu} \tag{2}$$

$$\mathcal{C}\psi\mathcal{C}^* = (\alpha_{\psi})^* C \bar{\psi}^T \qquad \qquad \mathcal{P}\psi\mathcal{P}^* = (\alpha_{\psi})^* \beta\psi, \qquad (3)$$

where ψ is a spinor and

$$C = \begin{bmatrix} -\epsilon & 0\\ 0 & \epsilon \end{bmatrix}, \qquad \epsilon = i\sigma_2 = \begin{bmatrix} 0 & 1\\ -1 & 0 \end{bmatrix}, \qquad \beta = \begin{bmatrix} 0 & 1\\ 1 & 0 \end{bmatrix}, \qquad (4)$$

show that:

- \mathcal{L}_q^W is not invariant under C ;
- \mathcal{L}_q^W is not invariant under P ;
- \mathcal{L}_q^W would be invariant under CP if the CKM-matrix were real.